Experimental and Theoretical Investigation of Unglazed Transpired Air Collectors in a Multicomponent Solar Thermal System

E. Frank, C. Budig, K. Vajen
Universität Kassel, Institut für thermische Energietechnik, 34109 Kassel, Germany
www.solar.uni-kassel.de, solar@uni-kassel.de

Abstract
Unglazed Transpired Air Collectors (UTC) are a simple and cost-effective technology to heat up ambient air, typically used in open solar air systems, e.g. for space heating of production halls. A new application is the air assisted preheating for district heating nets in the former Soviet Union. Due to the unusual operating conditions in this application an existing numerical model has been extended. The thermal performance of the UTC is modelled as a matrix of energy balance equations. The model has a wide area of application, since it covers already known standard applications as well as specific constructional and technical features of the collector. Furthermore, convective losses from the collector to the surrounding, the dependency of the absorption coefficient on the angle of incidence and the capacity of the building wall are considered. The presented model was implemented in the simulation environment TRNSYS and has been compared with measurement data.

Keywords: Unglazed Transpired Air Collector, Multicomponent System, Numerical model

1. Introduction
Unglazed Transpired Air Collectors (UTC) have been the subject of a number of investigations, e.g. [1, 2]. Typically, UTCs are used in open solar air systems to heat up ambient air. In the UTC, air adjacent to the front surface of the absorber is drawn through perforations of a dark-coloured, sun-warmed metal sheet (cf. Fig. 1).

In a cooperation project between Kassel University (Germany) and the Kyrgyz Technical University in Bishkek (Kyrgyzstan) a new kind of solar heating system (cf. Fig. 2) is being investigated theoretically and experimentally to preheat water for a district heating net [3]. In this multicomponent solar thermal system an UTC is installed on the facade to heat up an air flow above ambient temperature level. The hot air is further used to heat up water in an air-to-water heat exchanger (AHX). The UTC consists of a corrugated perforated absorber 1, an aluminium tray as side and back wall and a rectangular duct which connects the two UTC fields (total area A=31.5 m²). Unlike commercial applications, the UTC of the research plant consists of a long air channel connecting the UTC fields and the air-to-water heat exchanger to measure the air flow rate using a flow grid.

In contrast to standard applications the hot air flow of this UTC is used for the preheating of cold water so that the flow rate and by that the outlet air temperature are not constricted. Thus, the dimensions and the operation of the UTC can be laid out for maximum energy gain taking parasitic energy and system costs into account. In the experimental setup in Bishkek

---

1 The plate has 1.1mm diameter holes arranged in a triangular pattern with 0.6% open area.
the UTC is equipped with an additional back wall due to the building wall conditions. An air gap between the UTC back wall and the building wall results from this special construction.

Fig. 2. Experimental setup at a heat plant in Bishkek (Kyrgyzstan) (left) and the scheme of a serially connected multicomponent system with exemplary temperatures (right).

2. Extended numerical model for UTCs

Due to the unconventional boundary conditions of the application an extended numerical model was developed and compared to measurement data collected in Bishkek. The model was derived from existing models for facade-mounted UTCs using the building wall as back wall for the collector [4]. The temperatures of the absorber, the back wall of the collector, the building wall and the plenum are assumed to be uniform, therefore a homogenous flow across the whole collector area is presumed. The quality of these assumptions depends on the air flow rate: With higher flow rates, the difference between the temperatures at the top and bottom areas of the collector increases because the suction velocity at the top area of the collector is greater than at the bottom [5].

In the following, a 9x1-knot model is introduced consisting of three energy balance equations, rate and efficiency equations. The resulting system of equations can be solved numerically, thus determining the outlet temperature of the collector \( T_{\text{out}} \). Eqs. (1-3) describe the thermal performance of the UTC based on the energy balances of the perforated absorber, the back wall of the collector and the building wall (cf. Fig. 3). The capacities of the absorber and the back wall are neglected due to their low masses.

Rate equations for the energy flows are required in order to solve the energy balance equations. According to [6], the solar radiation absorbed by the collector \( Q_{\text{col.abs}} \), the energy flux between collector and back wall \( Q_{\text{col.back}} \), and losses to the environment via radiation \( Q_{\text{col.sur}} \) can be calculated directly (eqs. 4-6). The dependency of the absorption coefficient on the angle of incidence is approximated by a correlation typical for plane black surfaces [6] because it is unknown for corrugated UTCs, so far.

For corrugated transpired solar collectors, convective losses to the surrounding must not be neglected. Empirical studies of large UTC systems showed that the efficiency of UTCs is depending on the wind speed [7, 8]. Therefore, the Nusselt number \( \text{Nu}_{\text{air}} \) was determined numerically and experimentally [9]. Depending on the operating conditions, attached or separated boundary layers can occur at the absorber plate. Thermal losses for separated boundary layers are considerably greater than for attached layers. For both cases, [9] determines a specific Nusselt number correlation. For average suction face velocities \( v_{0} \geq 6,93 \cdot 10^{-1} \sqrt{\frac{\nu_{\text{air}}}{\nu_{w}}} \) eq. (8) has to be applied, otherwise eq. (9).

2 The labelling convention for heat flows is \( \dot{Q}_{\text{Mode}, \text{from/to}} \), where \( \text{Mode} \) denotes the heat transfer mechanism (\( \text{conv} \) for convection, \( \text{rad} \) for radiation, \( \text{abs} \) for absorption, \( \text{cap} \) for capacity) and \( \text{from/to} \) describe the source/destination of heat transfer, respectively.
As the ambient air passes over and through the absorber, it is heated up by the convective heat flow from the collector into the plenum. Thus, this heat flow can be calculated by eq. (10).

\[
\dot{Q}_{\text{conv, plen}} = \dot{m}_{\text{air}} c_{p, \text{air}} (T_{\text{plen}} - T_{\text{amb}})
\]
Eq. (2) is the energy balance for the back wall of the collector. Because of the small thickness and the low thermal resistance the back wall is modelled with a single temperature knot and its capacity is neglected.

While the air is passing through the perforated absorber it is heated up to the temperature \(T_{\text{plen}}\). If \(T_{\text{back}}\) is lower than \(T_{\text{plen}}\) the air flow in the collector to the top of the plenum is then cooled down to the outlet temperature \(T_{\text{out}}\) by a convective heat flow to the back wall. This heat flow can be expressed by the following eq. (11):

\[
\dot{Q}_{\text{conv, plen-back}} = \dot{m} \cdot c_{p,\text{air}} \cdot (T_{\text{plen}} - T_{\text{out}})
\]

(11)

The heat flows \(\dot{Q}_{\text{conv, plen-back}}\) and \(\dot{Q}_{\text{conv, back-gap}}\) can also be expressed in terms of their heat transfer coefficients:

\[
\dot{Q}_{\text{conv, plen-back}} = h_{\text{plen-back}} A (T_{\text{out}} - T_{\text{back}}) = \frac{\text{Nu}_{\text{plen-back}} \cdot k_{\text{air}}}{H} A (T_{\text{out}} - T_{\text{back}})
\]

(12)

\[
\dot{Q}_{\text{conv, back-gap}} = h_{\text{back-gap}} A (T_{\text{back}} - T_{\text{gap}}) = \frac{\text{Nu}_{\text{free}} \cdot k_{\text{air}}}{H} A (T_{\text{back}} - T_{\text{gap}})
\]

(13)

So far no systematic investigations have been carried out regarding the properties of the air flow in the plenum. Therefore, no specific heat transfer function exists so that an approximation for forced convection at parallel flat-plate airflows is applied. Free convection from the back wall of the collector to the air in the plenum is expressed by adapting known correlations for streams hitting vertically on a plane [10].

The radiation heat flow between the back wall of the collector and the building wall can be calculated analogous to eq. (5).

As shown in experimental results [11], the heat capacity of the building wall (cf. eq. (3)) can not be neglected. The capacity heat flow is calculated by eq. (14).

\[
\dot{Q}_{\text{cap, wall}} = m_{\text{wall}} c_{p,\text{wall}} \Delta T_{\text{wall}}
\]

(14)

The heat flows \(\dot{Q}_{\text{conv, wall-gap}}\) and \(\dot{Q}_{\text{conv, room-wall}}\) can be determined analogous to \(\dot{Q}_{\text{conv, back-gap}}\).

For solving the system of equations in eq. (15) the heat exchange effectiveness \(\varepsilon_{\text{Hx}}\) of the absorber is defined. \(\varepsilon_{\text{Hx}}\) can also be calculated by eq. (16) using the appropriate heat transfer coefficient. For the convectional heat transfer from the collector plate to the air flow in the plenum a Nusselt number is applied that was derived experimentally [12], cf. eq (17).

\[
\varepsilon_{\text{Hx}} = \left(\frac{T_{\text{plen}} - T_{\text{amb}}}{T_{\text{col}} - T_{\text{amb}}}\right)
\]

(15)

\[
\varepsilon_{\text{Hx}} = 1 - \exp\left(\frac{-\text{Nu}_{\text{col-plex}} \cdot k_{\text{air}} \cdot (1 - \kappa)}{D \cdot \rho_{\text{air}} \cdot v_{\theta} \cdot c_{p,\text{air}}}\right)
\]

(16)

\[
\text{Nu}_{\text{col-plex}} = 2.75 \cdot \left(\frac{P}{D}\right)^{1.2} \cdot \text{Re}^{0.43}_{D}
\]

(17)

3. Selected simulation results

The presented UTC model was implemented into the simulation environment TRNSYS. Calculations have been carried out for conditions as they can be found in the application in Bishkek using values from literature or manufacturer’s specifications for absorption coefficients, emissivities etc.. Fig. 4 shows the simulated efficiency and air temperature rise of the unglazed transpired collector as a function of air flow rate for no wind and a wind speed of 5m/s. Especially for low specific air flow rates in the range of 100m³h⁻¹m⁻² the collector efficiency varies significantly depending on the wind conditions, which corresponds with experimental data. Further analysis of the modelled heat flows with low air flow rates and a wind speed of 5m/s showed that losses by convective heat flow are significant and in the range of heat losses by radiation (cf. Table 1).
Fig. 4. Efficiency (left axis) and air temperature rise (right axis) of an unglazed transpired collector as a function of air flow rate for no wind and a wind speed of 5 m/s (global irradiation = 900 W/m², ambient temperature = 32°C and sky temperature = 7°C).

Table 1. Heat flow ratios of the perforated absorber for low air flow rates (120 m³/h·m⁻²).

<p>| | | | | | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>( \dot{Q}_{\text{abs}} )</td>
<td>( \dot{Q}_{\text{rad, col - sur}} )</td>
<td>( \dot{Q}_{\text{conv, col - sur}} )</td>
<td>( \dot{Q}_{\text{conv, col - plen}} )</td>
<td>( \dot{Q}_{\text{rad, col - back}} )</td>
<td></td>
</tr>
<tr>
<td>0 m/s</td>
<td>100 %</td>
<td>25,4 %</td>
<td>0 %</td>
<td>67,7 %</td>
<td>6,9 %</td>
<td></td>
</tr>
<tr>
<td>5 m/s</td>
<td>100 %</td>
<td>20,6 %</td>
<td>23,9 %</td>
<td>50,5 %</td>
<td>5,0 %</td>
<td></td>
</tr>
</tbody>
</table>

4. Conclusions and Outlook

An extended numerical model has been developed for unglazed transpired air collectors with unusual operating conditions. The model covers already known standard applications as well as specific features of the collector. Especially, convective losses from the collector to the surrounding, the dependency of the absorption coefficient on the angle of incidence and the capacity of the building wall are considered. The simulation results are consistent with first experimental data collected in Bishkek. Thereby values of the absorption coefficients, the emissivities etc. have been taken from literature or manufacturer’s specifications. In a next step the model parameters will be determined using experimental data.

Acknowledgements

The authors would like to express their gratitude to the following institutions for their financial and logistical support: The VolkswagenStiftung (Germany) which funds the research project, the Center of the Problems of Unconventional and Renewable Energy Sources (Kyrgyzstan), the Kyrgyz Technical University in Bishkek, and the district heating net operator Bishkekteploenergo (Kyrgyzstan).

Nomenclature

\[ A = \text{collector face area, } m^2 \]
\[ c_{p, \text{air}} = \text{specific heat of air, } J \,(kgK)^{-1} \]
\[ c_{p, \text{wall}} = \text{specific capacity of the building wall, } J \,(kgK)^{-1} \]
\[ D = \text{collector hole diameter, } m \]
\[ G_r = \text{radiation incident on collector, } W/m^2 \]
\[ H = \text{height of the air collector, } m \]
\[ h = \text{heat transfer coefficient, } Wm^{-2}K^{-1} \]
\[ k_{\text{air}} = \text{thermal conductivity of air, } Wm^{-1}K^{-1} \]
\[ m_{\text{wall}} = \text{mass of building wall, kg} \]
\( \dot{m}_{\text{air}} \) = mass flow rate of air, kg/s
\( \text{Nu}_{\text{lost}} \) = Nussel number for corrugated plates
\( \text{Nu}_{\text{lost,att}} \) = Nussel number for corrugated plates in attached flow
\( \text{Nu}_{\text{lost,sep}} \) = Nussel number for corrugated plates in separated flow
\( \text{Nu}_{\text{plen-back}} \) = Nussel number for forced convection
\( \text{Nu}_{\text{free}} \) = Nussel number for free convection
\( \dot{Q}_{\text{stea, from-to}} \) = heat flow, W
\( \dot{Q}_{\text{cap,wall}} \) = heat capacity flow of building wall, W
\( \text{Re} \) = Reynolds number
\( T_{\text{amb}} \) = ambient air temperature, K
\( T_{\text{back}} \) = backside plate temperature, K
\( T_{\text{col}} \) = collector surface temperature, K
\( T_{\text{gap}} \) = air temperature of the air gap, K
\( T_{\text{out}} \) = collector outlet temperature, K
\( T_{\text{plen}} \) = plenum air temperature, K
\( T_{\text{room}} \) = room temperature, K
\( T_{\text{sky}} \) = sky temperature, K
\( T_{\text{sur}} \) = \( 0.5 \left( T_{\text{sky}}^1 + T_{\text{sur}}^1 \right) \)\(^{0.25} \) = surroundings temperature, K
\( \dot{T}_{\text{wall}} \) = alteration of the wall temperature, K/s
\( \dot{V}_{\text{air}} \) = air flow rate, m\(^3\)/s
\( \dot{v}_{\text{v}} \) = average suction face velocity, m/s
\( v \) = wind speed, m/s
\( \gamma \) = amplitude of corrugations, m
\( \alpha \) = absorption coefficient of collector
\( \alpha(\Theta) / \alpha_\perp \) = dependency of the absorption coefficient on the angle of incidence
\( \sigma \) = Stefan-Boltzmann constant
\( \varepsilon_{\text{back}} \) = emissivity of backside of the collector
\( \varepsilon_{\text{col}} \) = collector emissivity
\( \varepsilon_{\text{col,plen}} \) = collector emissivity towards the plenum
\( \varepsilon_{\text{Hx}} \) = heat exchanger effectiveness of collector
\( \varepsilon_{\text{w}} \) = emissivity of the building wall
\( \kappa \) = collector porosity
\( \lambda \) = wavelength of corrugations, m
\( \nu \) = kinematic viscosity of air, m\(^2\)/s
\( \rho_{\text{air}} \) = density of air, kg/m\(^3\)
\( \Theta \) = angle of incidence, °

References